

Millimeter-imaging spectrometer using magnetic field tunable kinetic inductance detectors (H-KID)

Florence Levy-Bertrand, solid state physicist (Institut Néel, Grenoble)

Work within the Scientific Interest Group on KIDs with



M. Calvo, J. Goupy, U. Chowdhury, A. Monfardini
B. Sacépé, G. Donnier-Valentin, T. Gandit



A. Gomez



Financial support

Millimeter-imaging spectrometer using magnetic field tunable kinetic inductance detectors (H-KID)

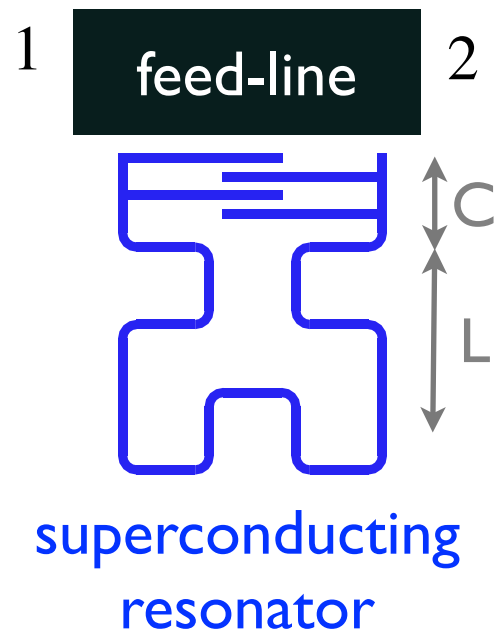
- Working principle of KID
- Magnetic field effect on KID: H-KID
- Toward a real mm-spectrometer with H-KID ?

Working principle of KID

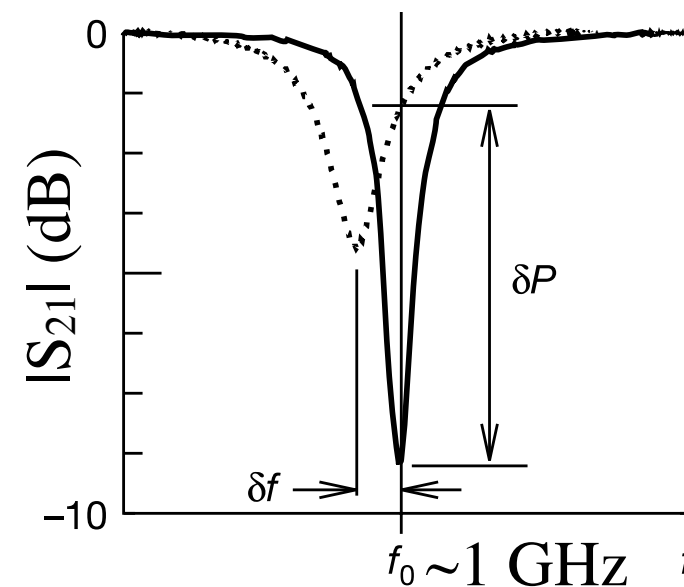
Day et al, Nature 425, 817 (2003)

Planar superconducting LC resonator on an insulating substrate

design



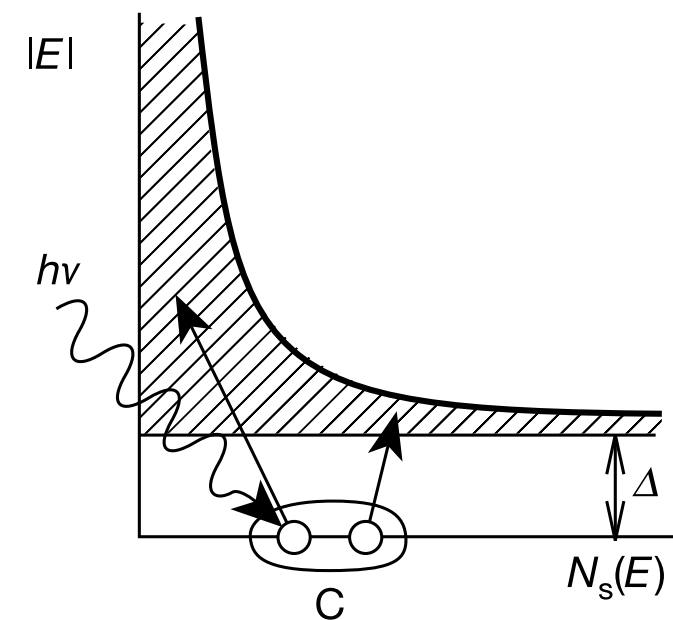
RF-electrical measurement



$$f_0 \sim (LC)^{-1/2}$$

photon detection principle :

$$h\nu > 2\Delta$$



L ~ kinetic inductance of the superfluid

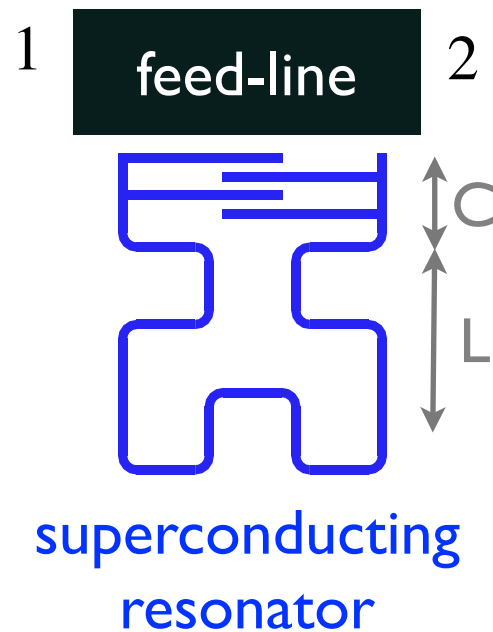
$$L \sim 1/n_s$$

Working principle of KID

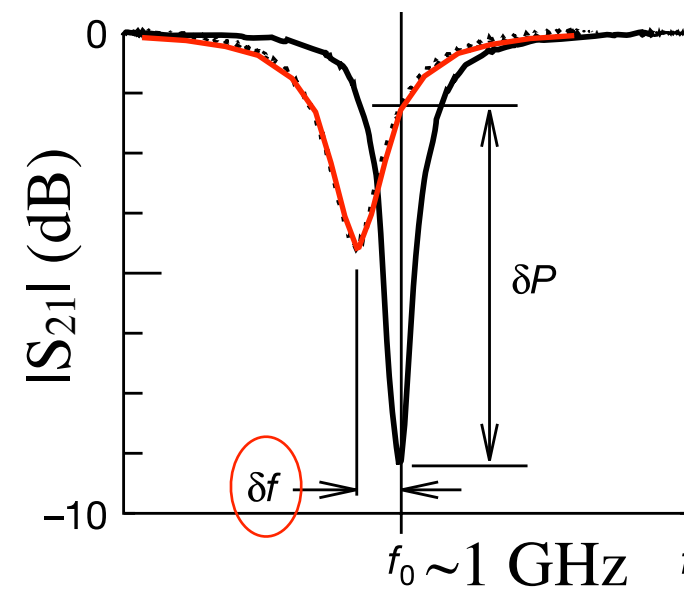
Day et al, Nature 425, 817 (2003)

Planar superconducting LC resonator on an insulating substrate

design



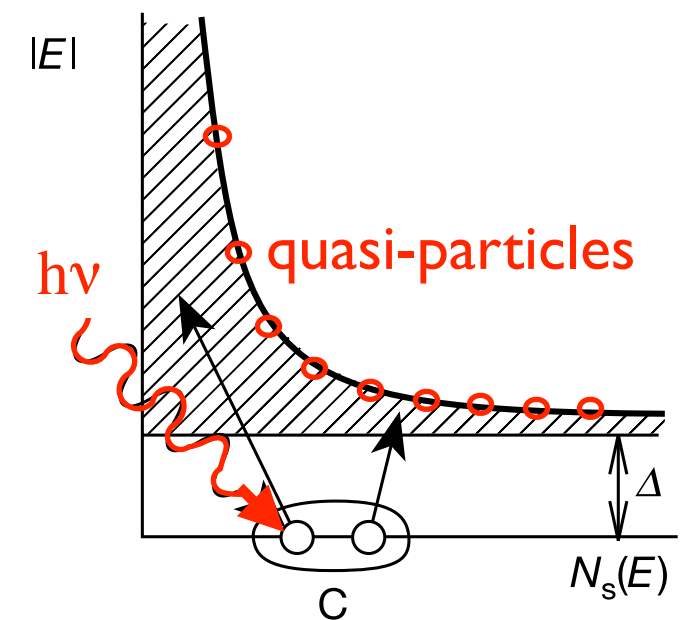
RF-electrical measurement



$$f_0 \sim (LC)^{-1/2}$$

photon detection principle :

$$h\nu > 2\Delta$$



frequency shift: δf due to $n_s \downarrow$

Q-factor \downarrow due to dissipation \uparrow

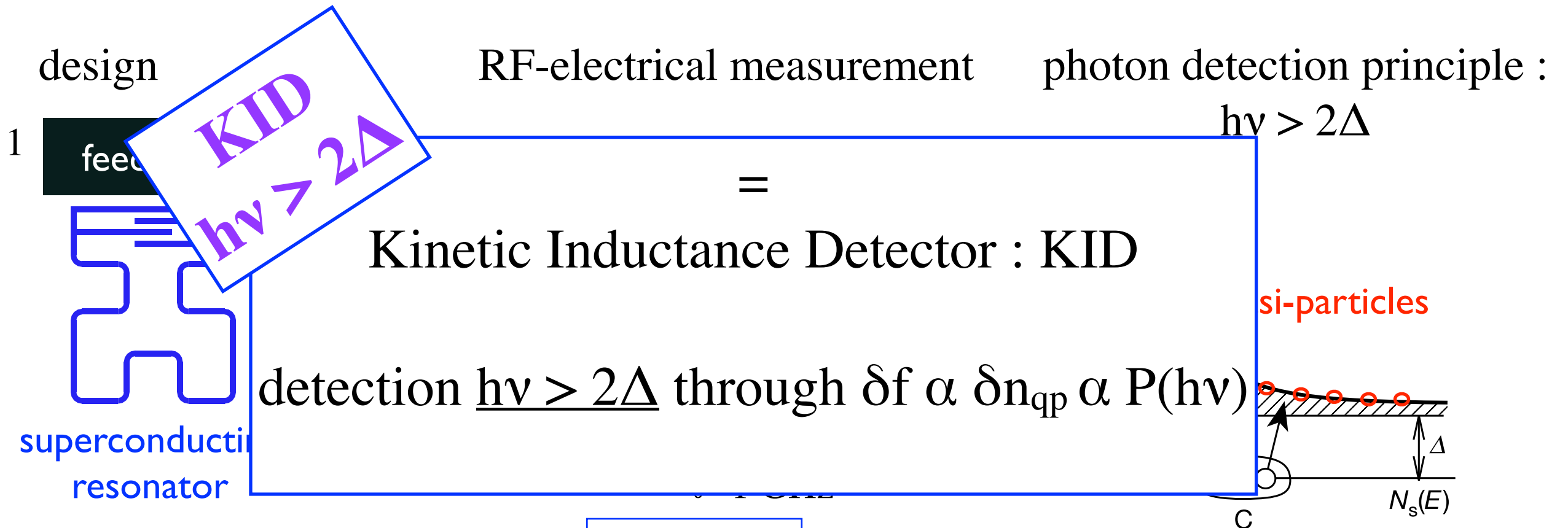
$L \sim$ kinetic inductance of the superfluid

$$L \sim 1/n_s$$

Working principle of KID

Day et al, Nature 425, 817 (2003)

Planar superconducting LC resonator on an insulating substrate



$$f_0 \sim (LC)^{-1/2}$$

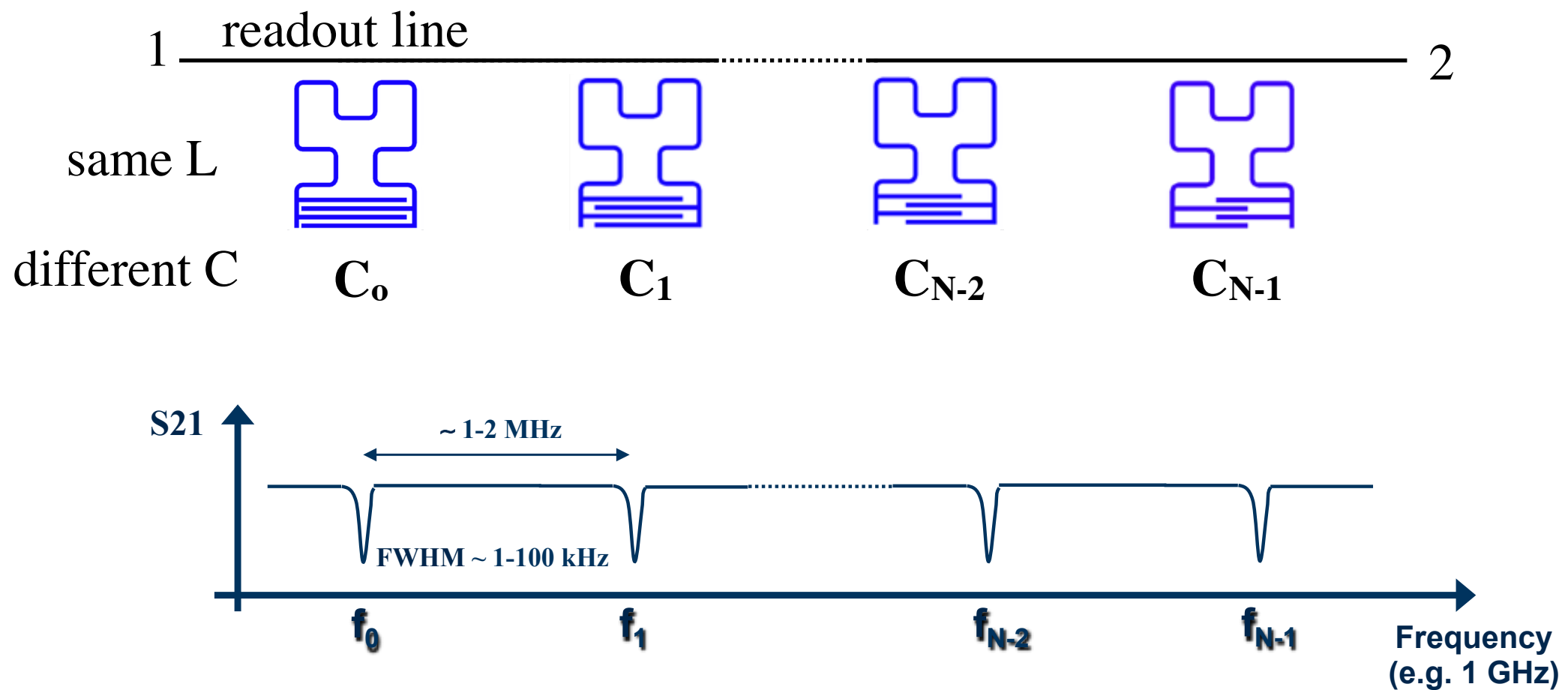
L ~ kinetic inductance of the superfluid
 $L \sim 1/n_s$

frequency shift: δf due to $n_s \downarrow$

Q-factor \downarrow due to dissipation \uparrow

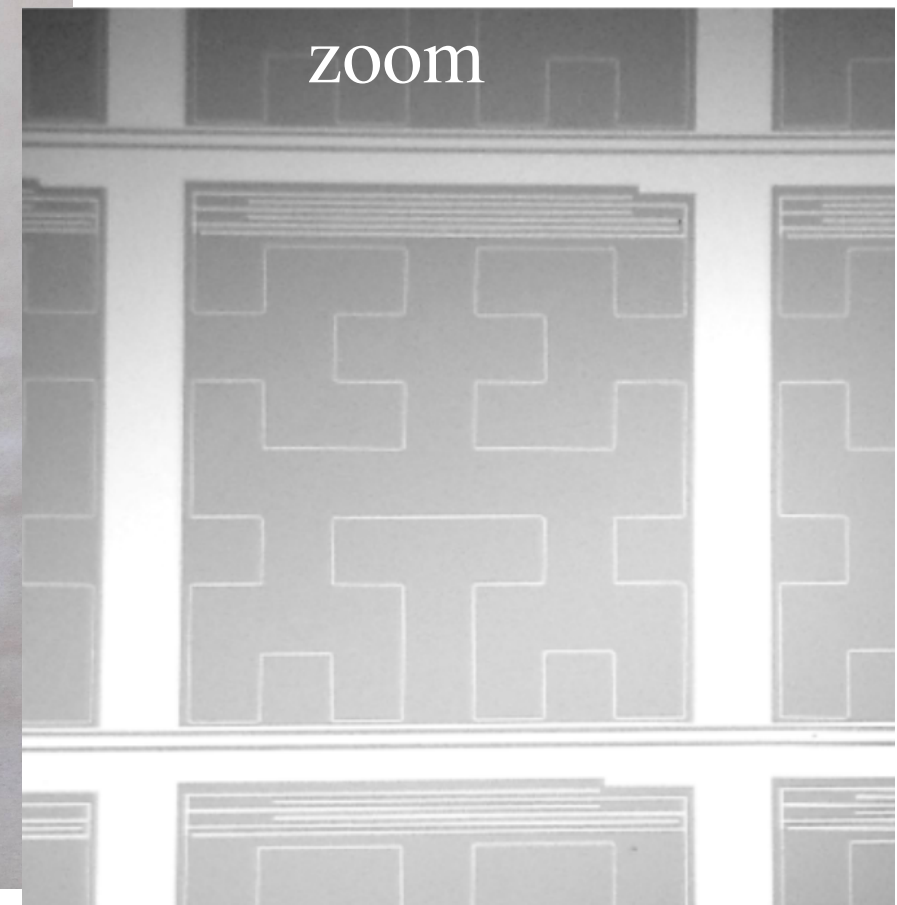
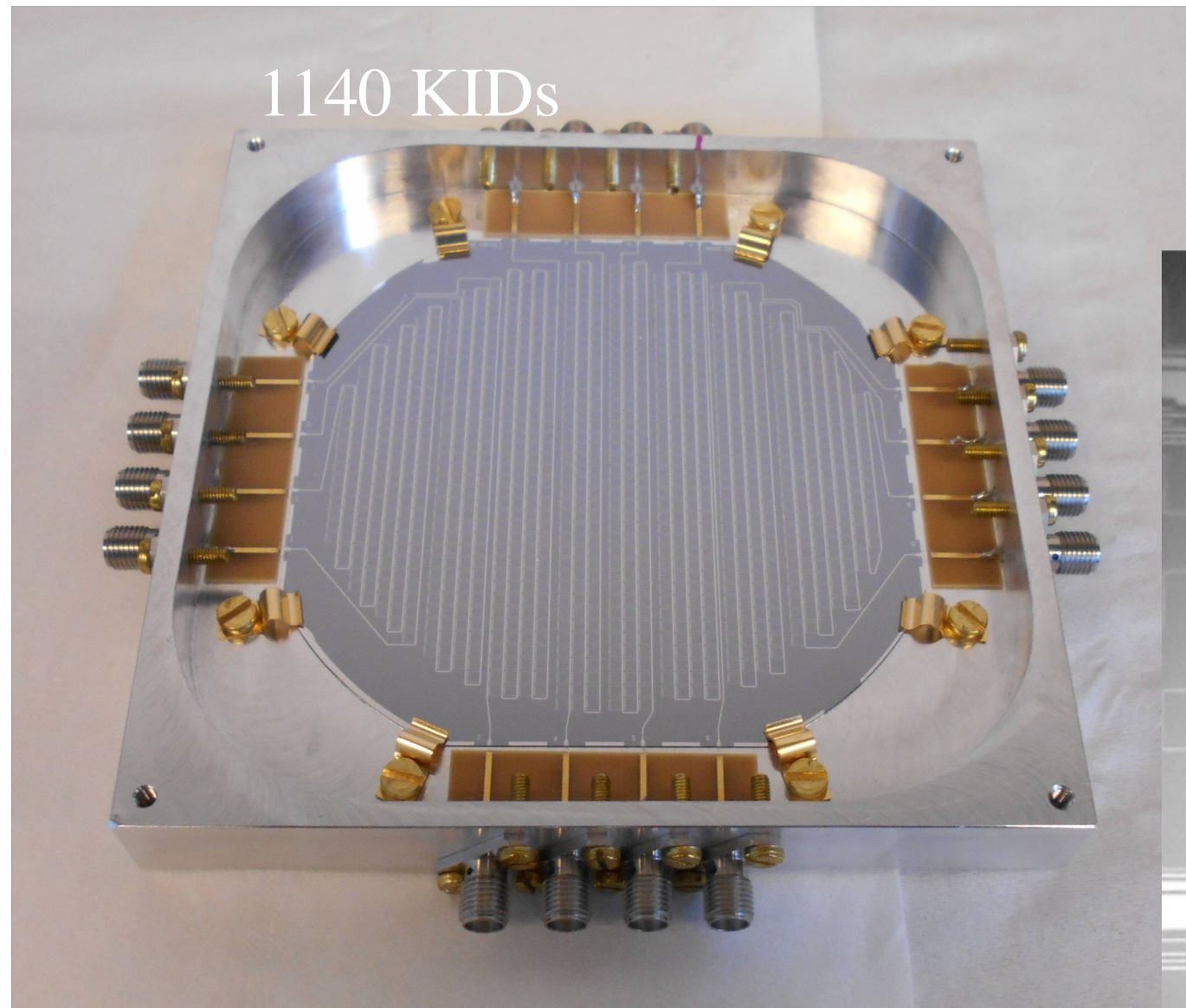
Working principle of KID

Frequency multiplexing: $f \sim (LC)^{-1/2}$



-> one line to address hundreds of detectors

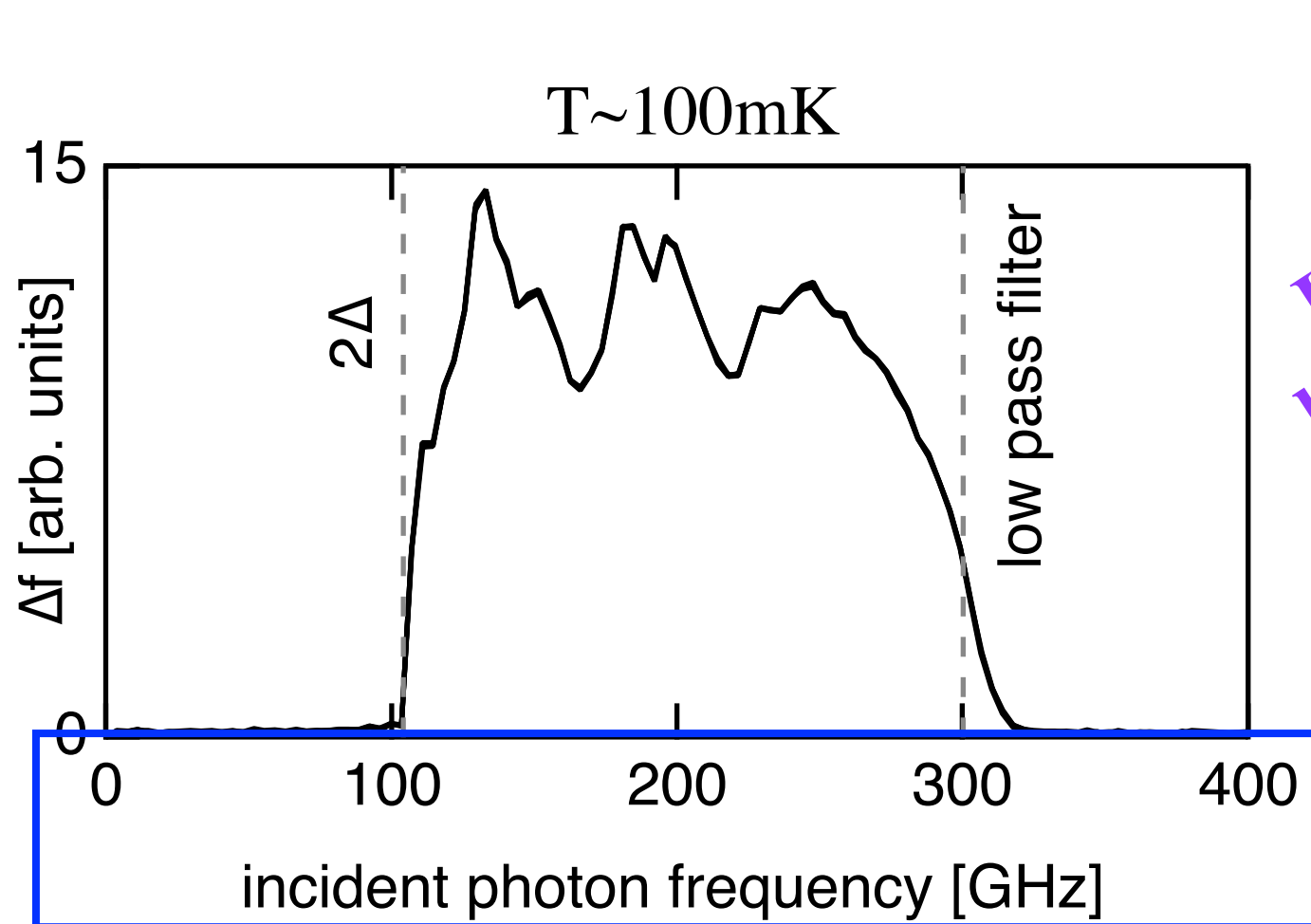
Working principle of KID



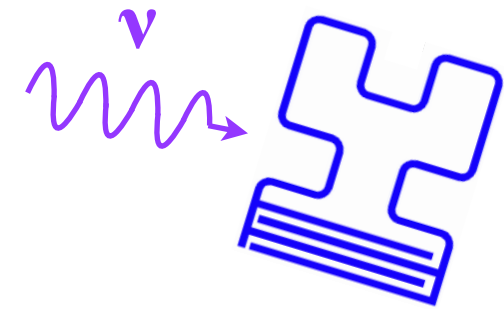
-> one line to address hundreds of detectors

Working principle of KID

Optical response of KID made of 20nm-thick Al



KID
 $h\nu > 2\Delta$



No sub-gap response.

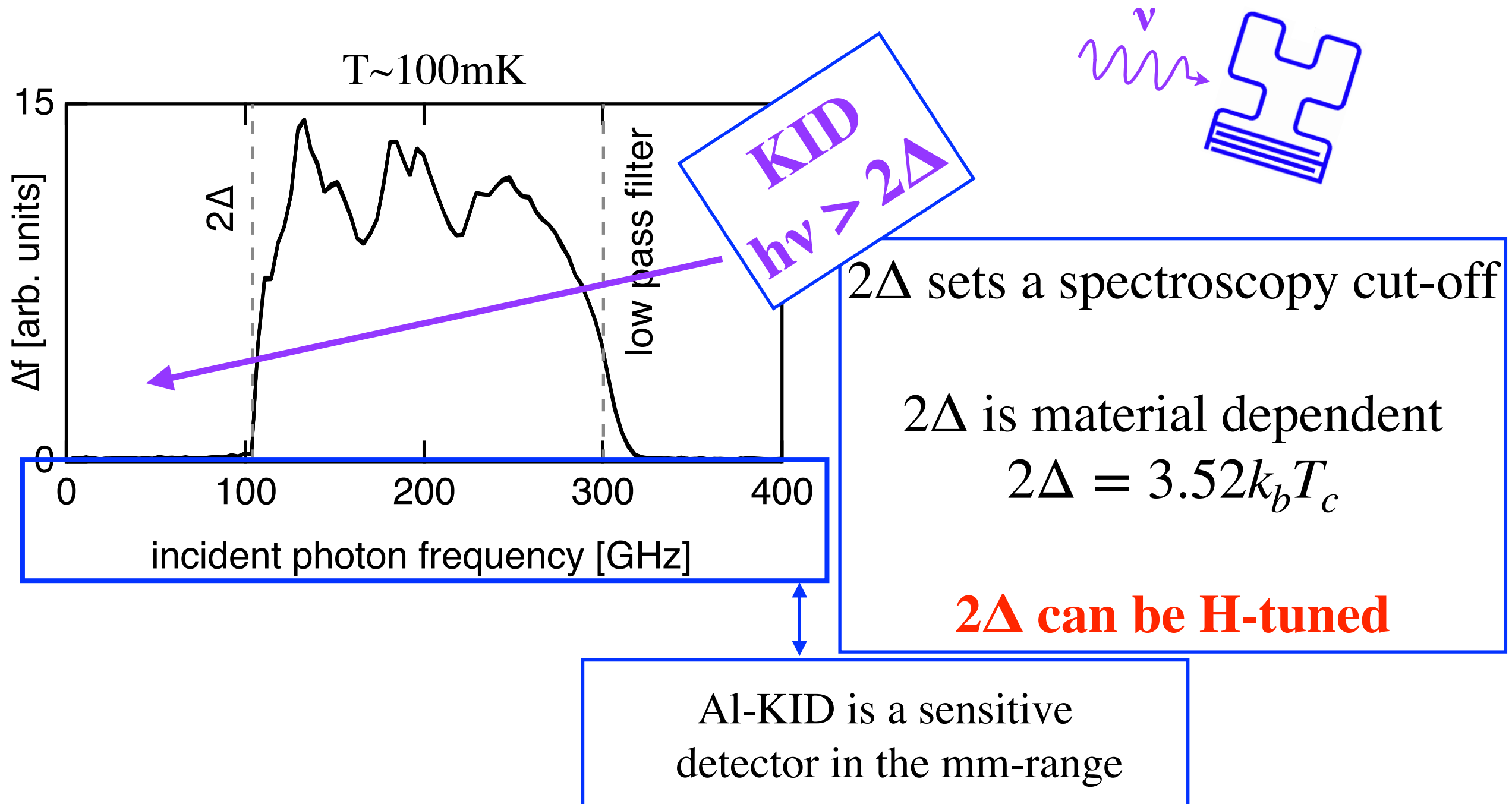
Incoming photons
break Cooper pairs.

$$\nu_{min} = 2\Delta/h$$

Al-KID is a sensitive
detector in the mm-range

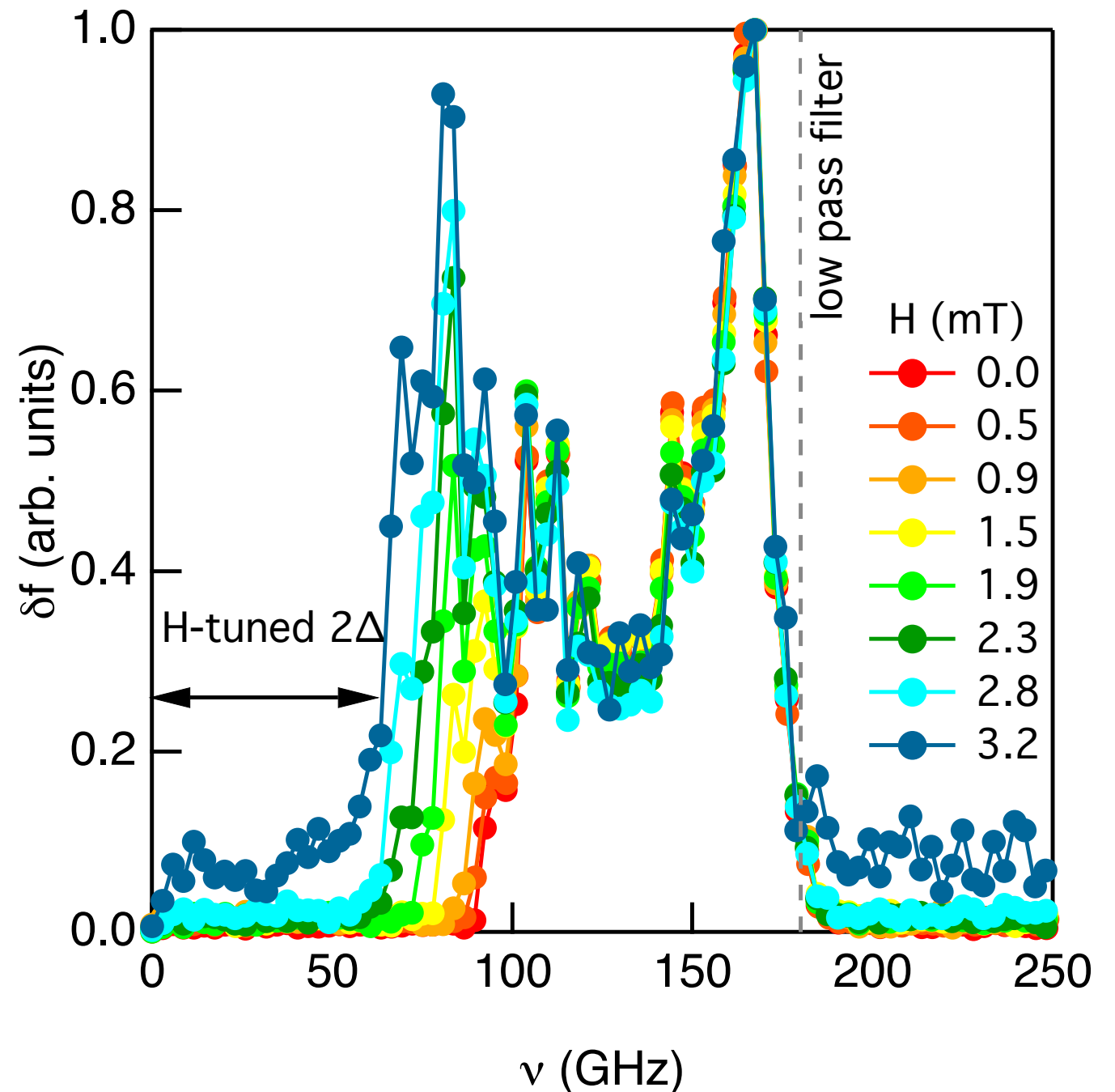
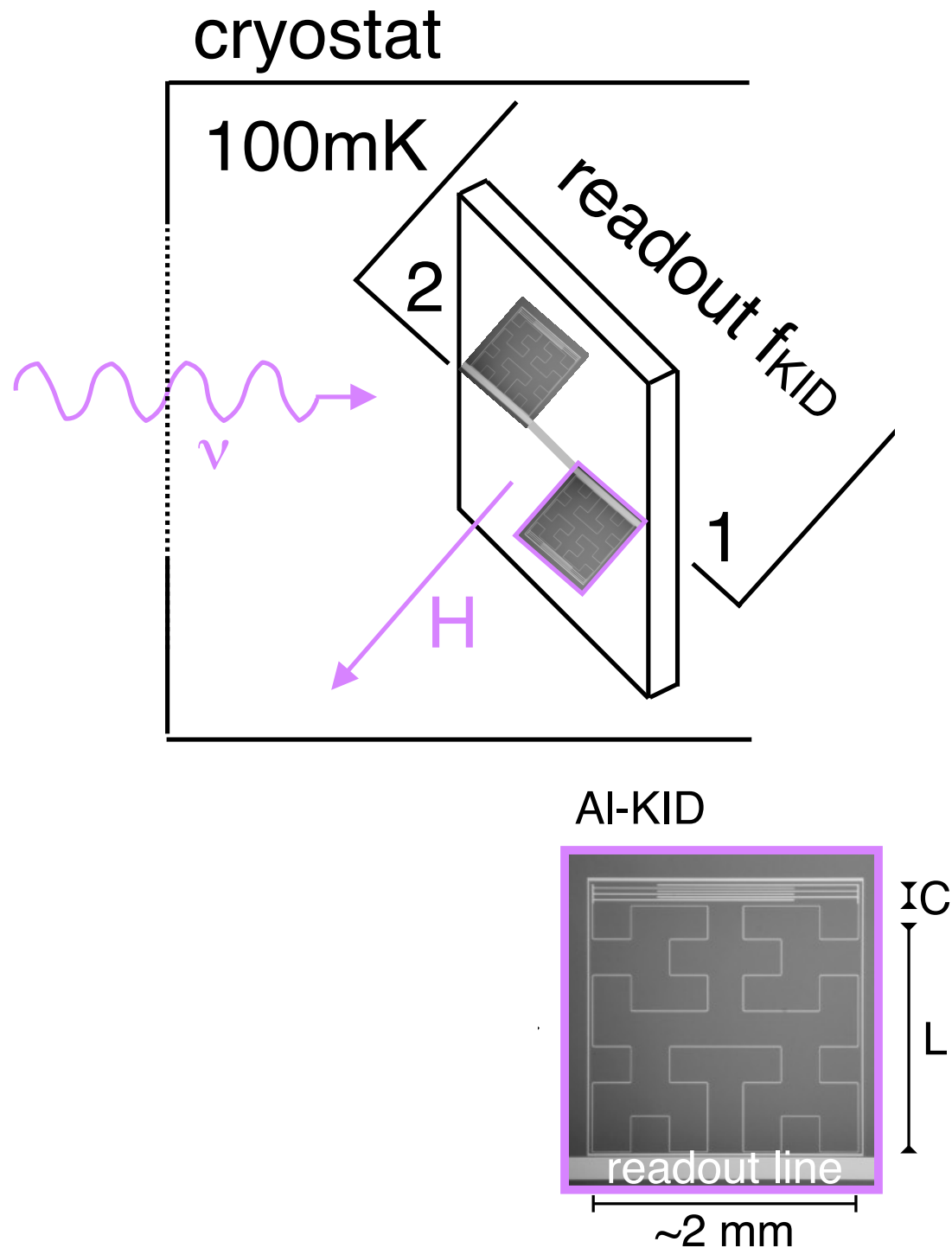
Working principle of KID

Optical response of KID made of 20nm-thick Al



Magnetic field effect on KID: H-KID

KID made of 200nm-Al, perpendicular H



Magnetic field effect on KID: H-KID

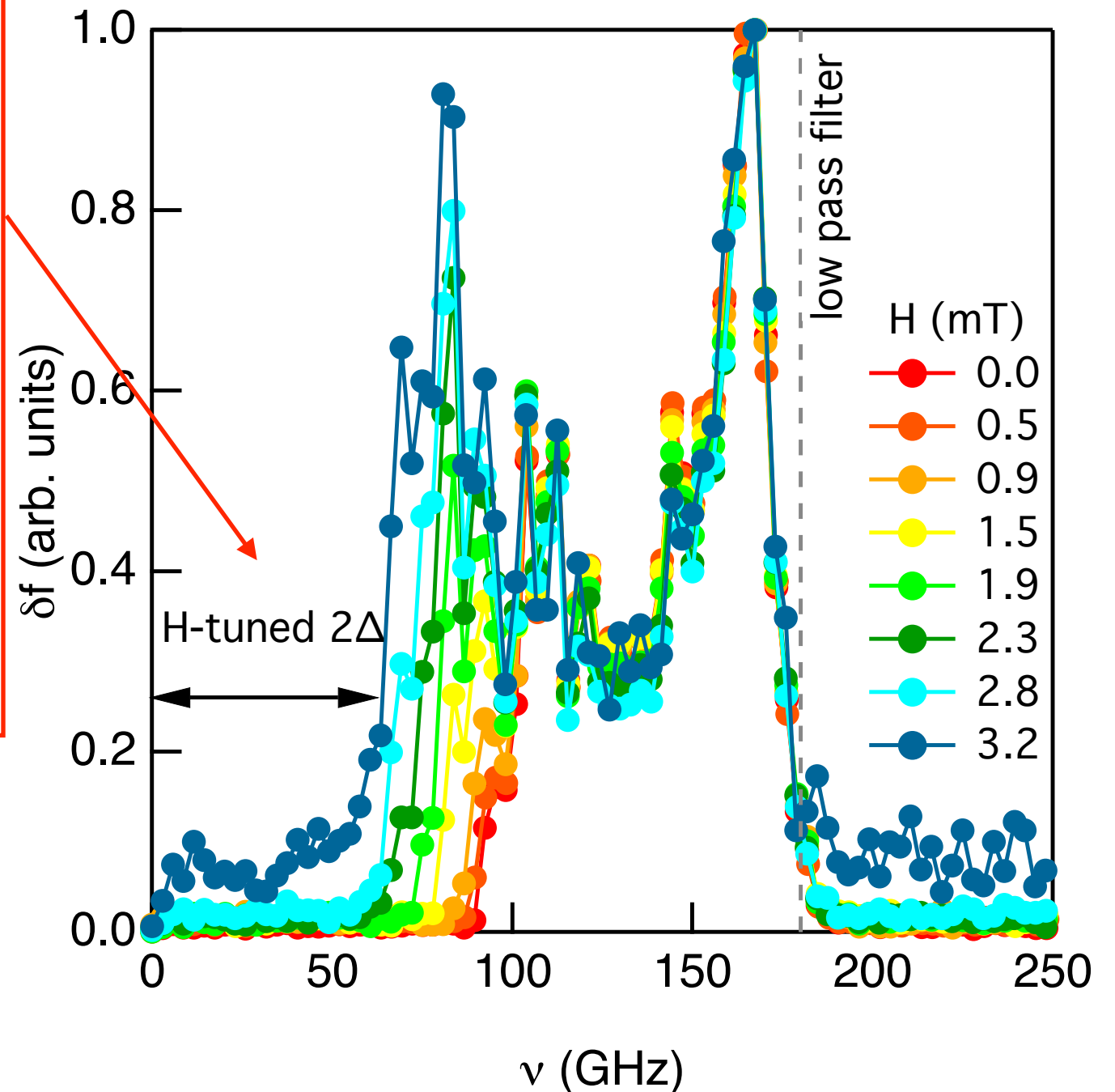
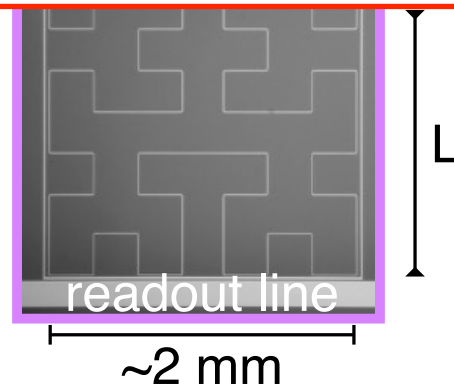
KID made of 200nm-Al, perpendicular H

H-tuned 2Δ

possible spectroscopy
with different ν -bands ?

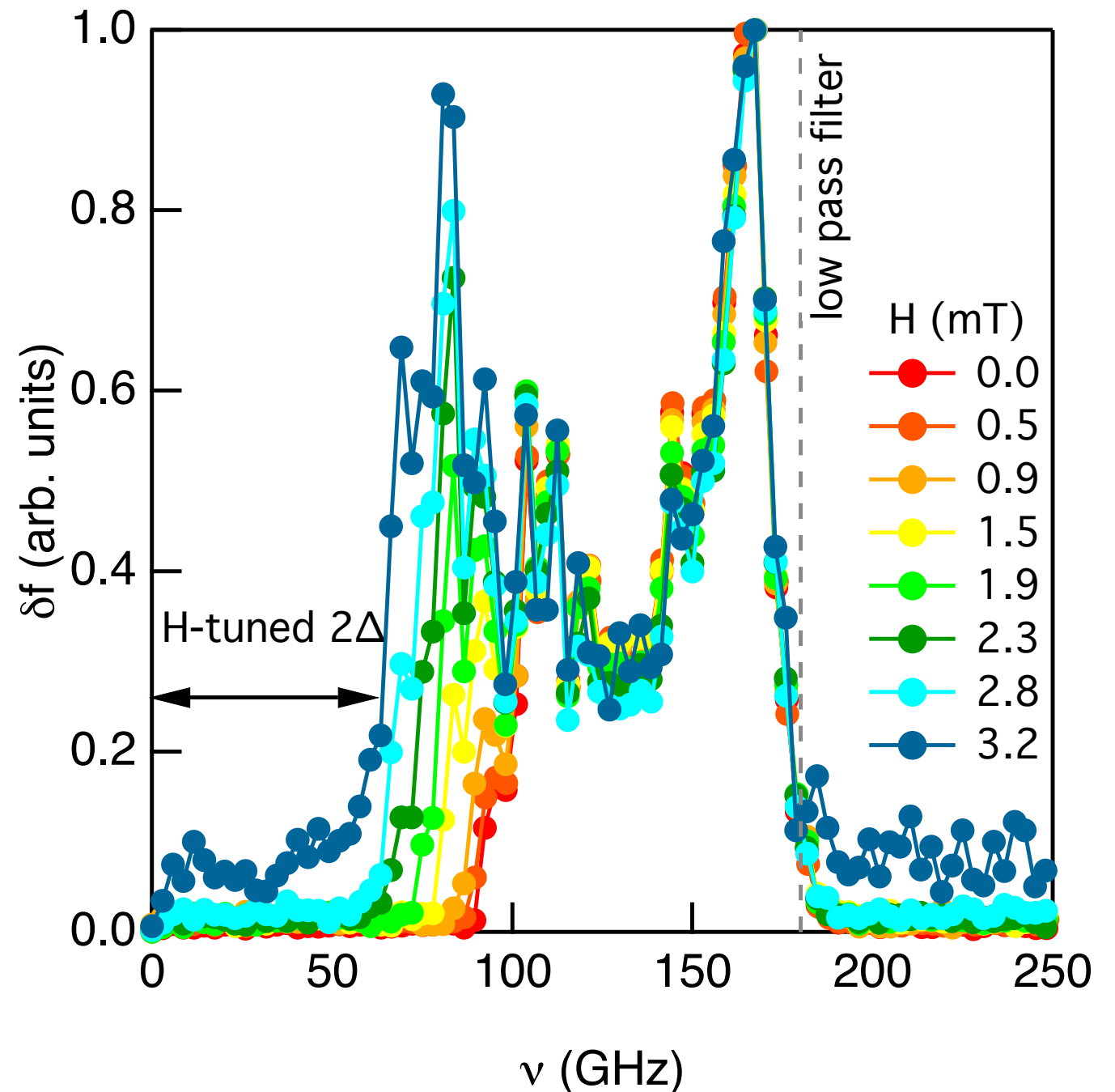
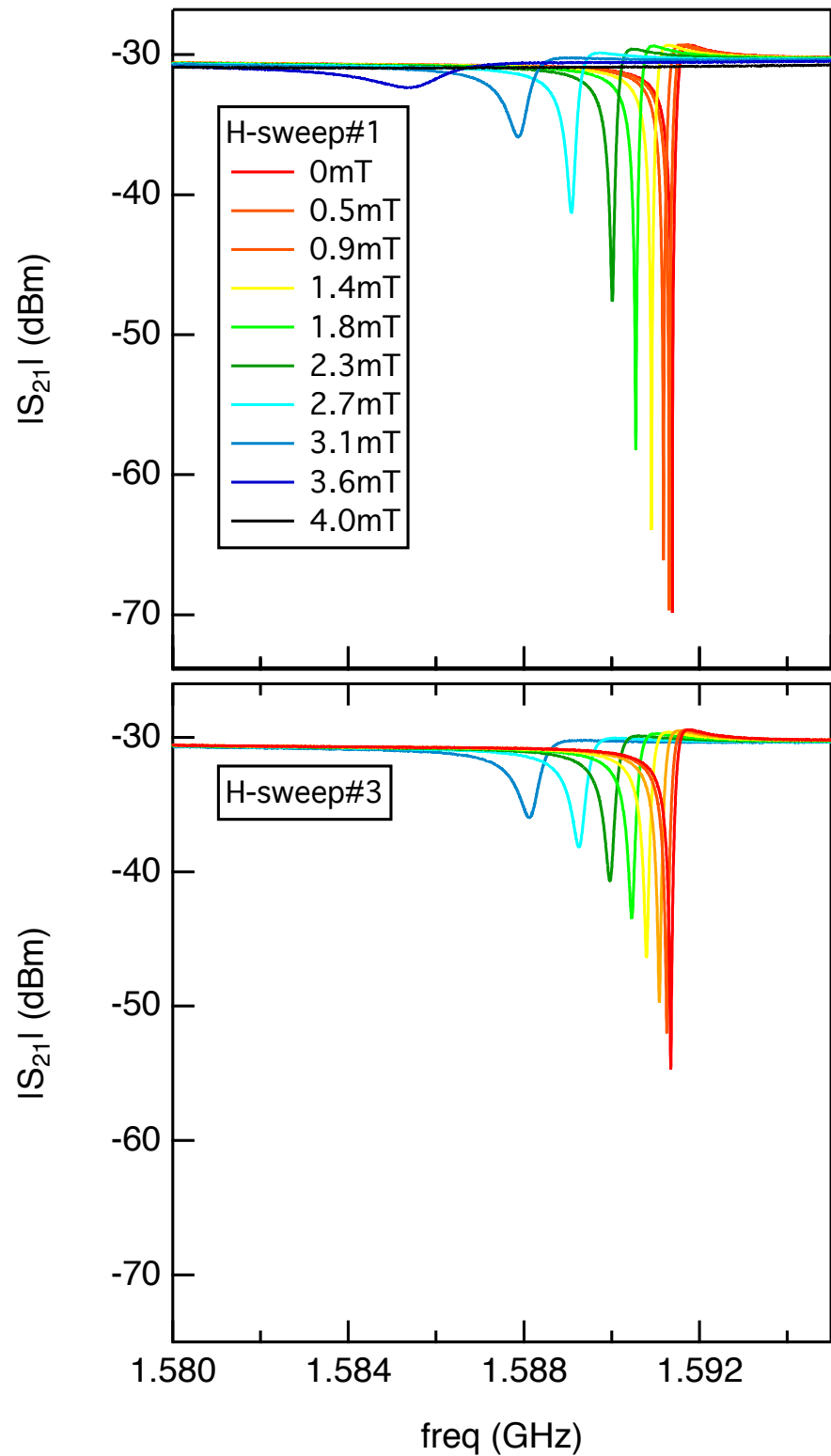
BUT

some constraints to overcome
related to H



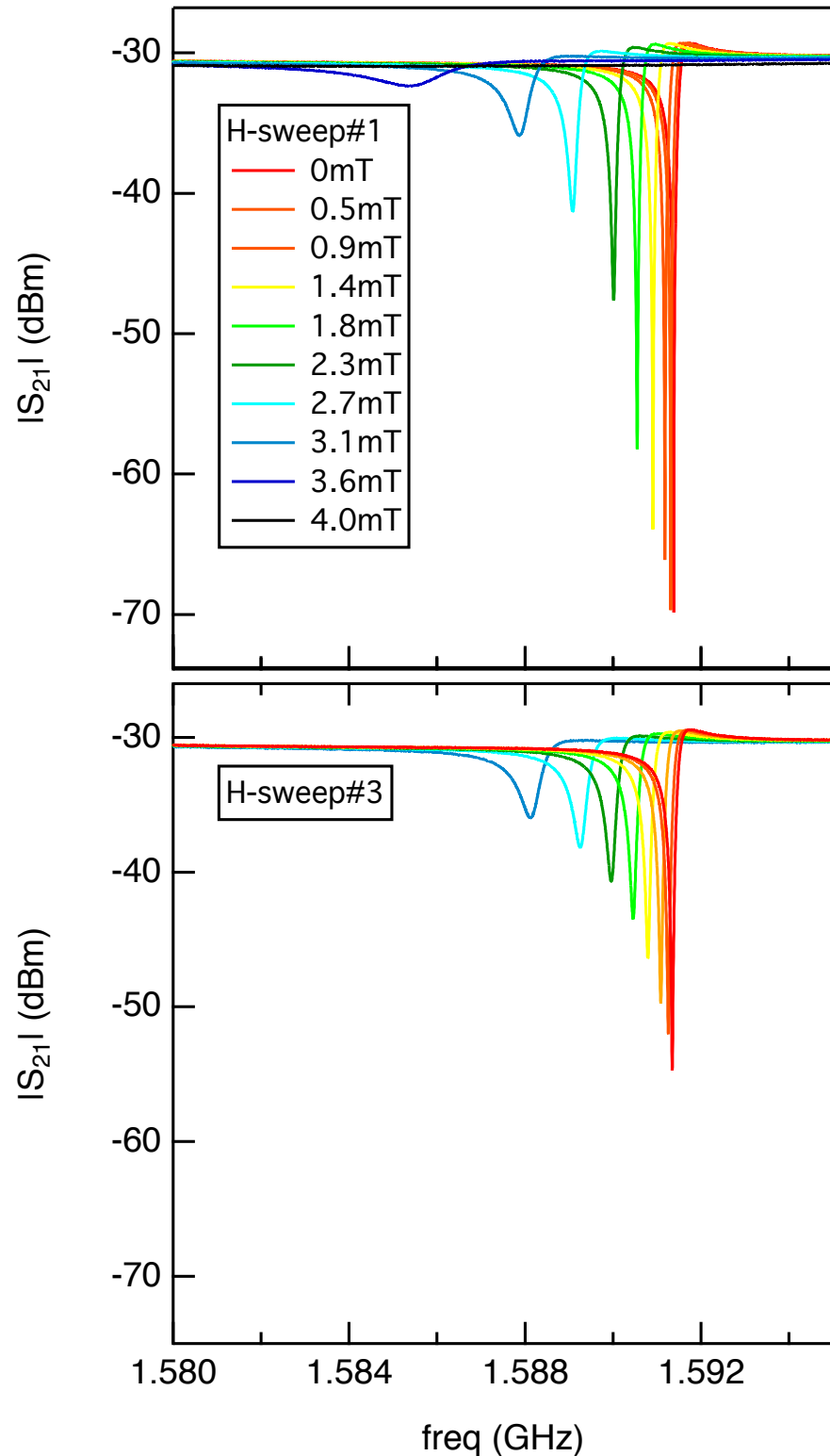
Magnetic field effect on KID: H-KID

KID made of 200nm-Al, perpendicular H



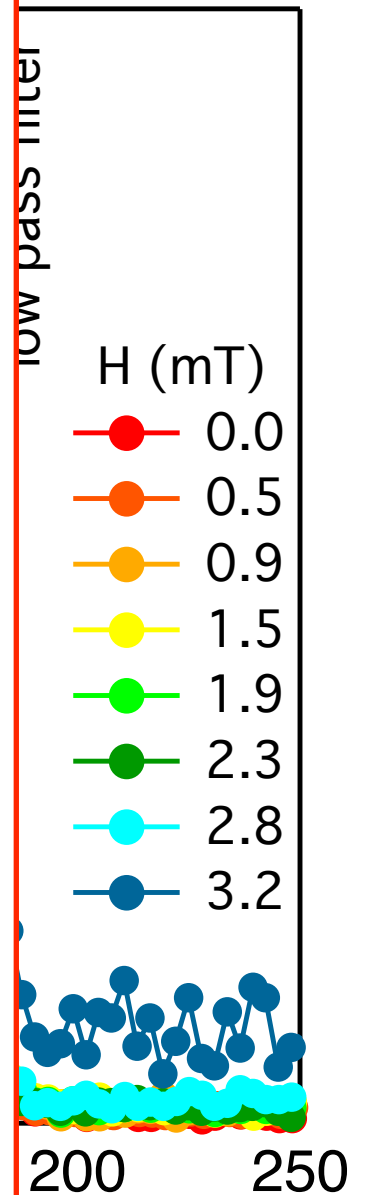
Magnetic field effect on KID: H-KID

KID made of 200nm-Al, perpendicular H



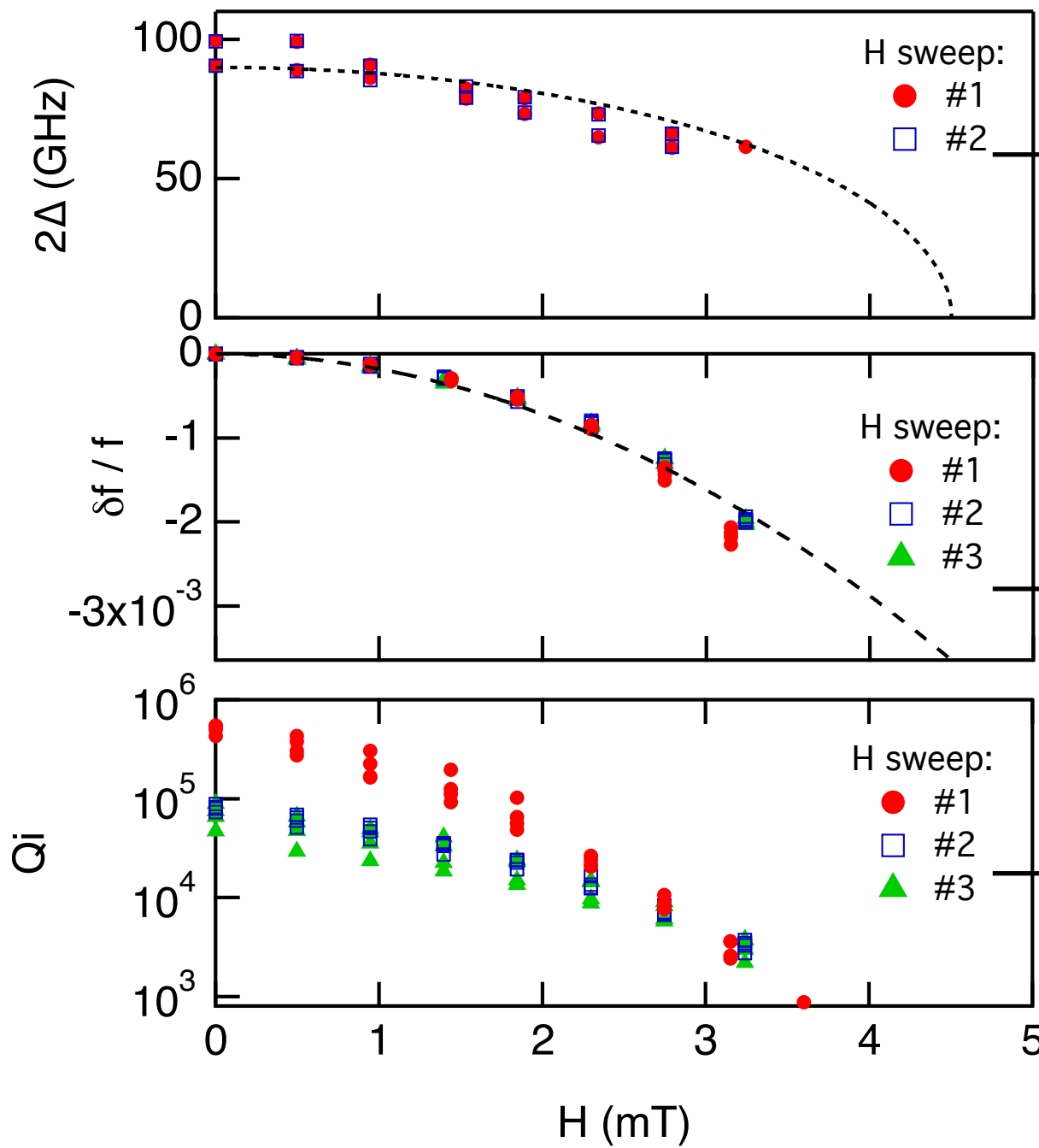
Constraints to overcome:

- f-variation with H
 - > reproducible
 - > calibration: **possible**
 - Q-variation with H
 - > vary with H-history
 - > calibration: **impossible**
 - > **Q too low** for $H/H_c > 0.6$
- ... due to vortex effect



Magnetic field effect on KID: H-KID

KID made of 200nm-Al, perpendicular H



$$\Delta(H) = \Delta_0 \sqrt{1 - \left(\frac{H}{H_c}\right)^2}$$

$$\frac{\delta f}{f} = -KH^2$$

vortex effect

Magnetic field effect on KID: H-KID

What is a vortex?

Supercurrent circulating around a **normal core**.

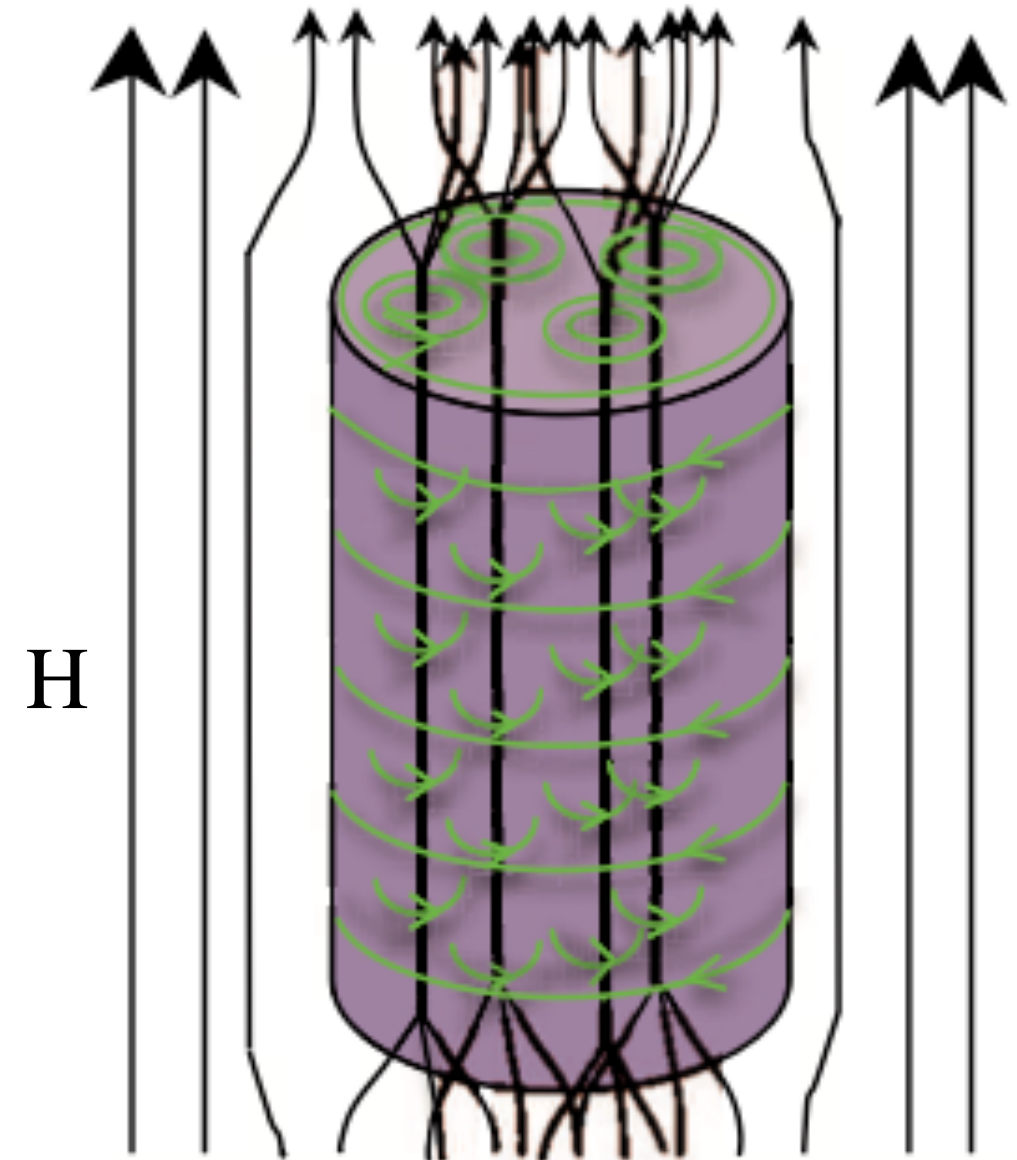
The vortex carries a quantum of magnetic flux $\phi_0 = h/(2e)$.

The vortex size is ξ .

Why a vortex generates dissipation ?

Because of the **movement** of the **normal electrons** of the vortex core.

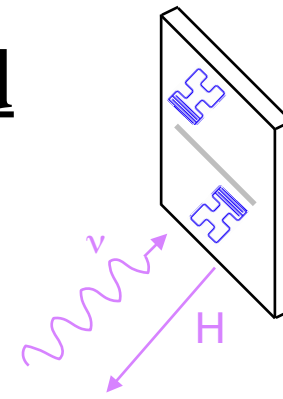
For a resonator, the vortex motion is due to the alternative current at ~ 1 GHz (Lorentz force).



Toward a real mm-spectrometer with H-KID

Vortex issue for perpendicular field

$$\text{Vortex for : } H > \frac{\pi\phi_0}{4w^2}$$



$\phi_0 = h/(2e)$ is the magnetic flux quantum

w is the width of the resonator

Magnetic earth field : 0.05 mT, vortex for $w > 5-6 \mu\text{m}$.

For Al 15nm, $2\Delta_0 = 110 \text{ GHz}$, $H_c = 40 \text{ mT}$,

$2\Delta_{\text{min}} = 55 \text{ GHz}$ corresponds to $H = 35 \text{ mT}$

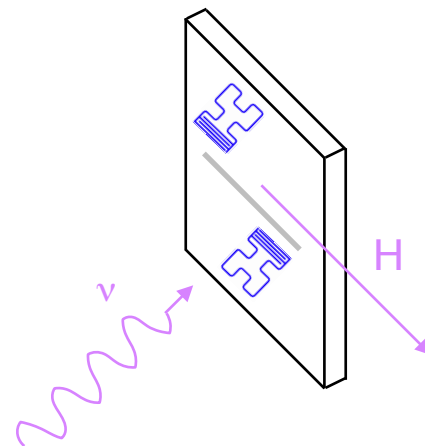
No vortex for $w = 200 \text{ nm}$

-> Challenge: **w = 200 nm**, possible with electronic lithography

Toward a real mm-spectrometer with H-KID

Vortex issue for parallel field

$$\text{Vortex for : } H > \frac{\pi\phi_0}{4w^2}$$



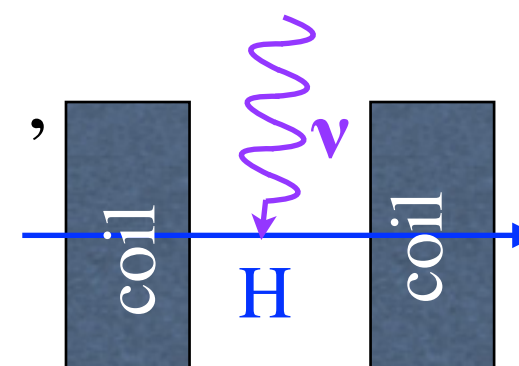
w is the thickness of the resonator

For Al 15nm, $H_{\parallel} \sim 20 - 100 H_{\perp} \sim 0.8 - 4 \text{ T}$ (???)

$2\Delta_{\min}=55 \text{ GHz}$ corresponds to $H=0.7-3.5 \text{ T}$

No vortex for « w » = 15 nm up to $H=7 \text{ T}$

-> Challenge: **Helmutz coil generating up to 1-4 T**, compatible with cryogenic environnement ...

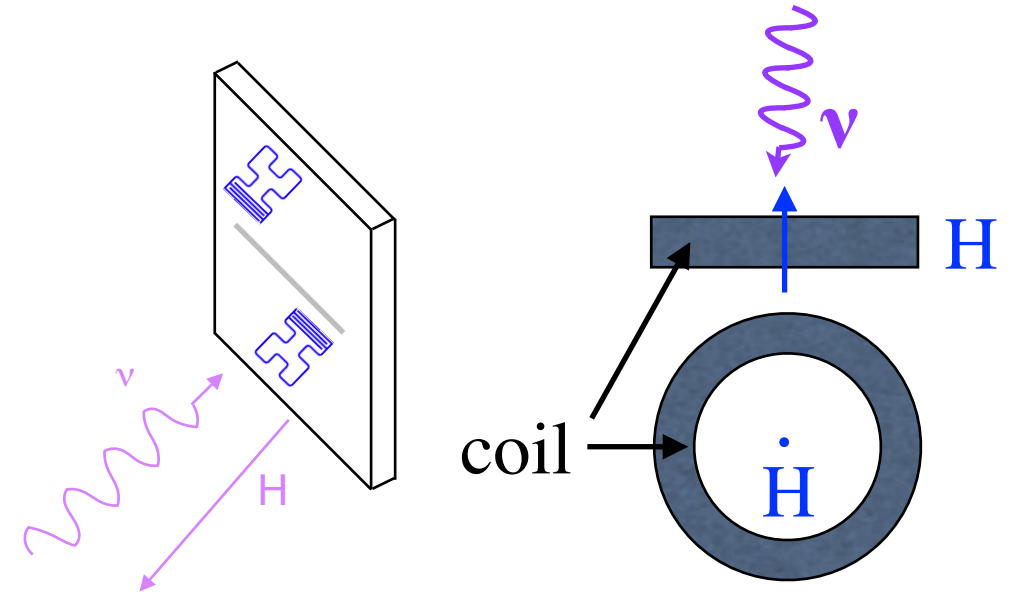


Toward a real mm-spectrometer with H-KID

Magnetic field issue for perpendicular field

$$\text{Standard coil : } H = \frac{\mu_0 I}{2r} N$$

μ_0 : vacuum permeability, I: current,
r: coil diameter, N: number of turns



Ex: $r=20\text{cm}$, $I=1\text{A}$, $N=100$, $H=0.3\text{mT}$.

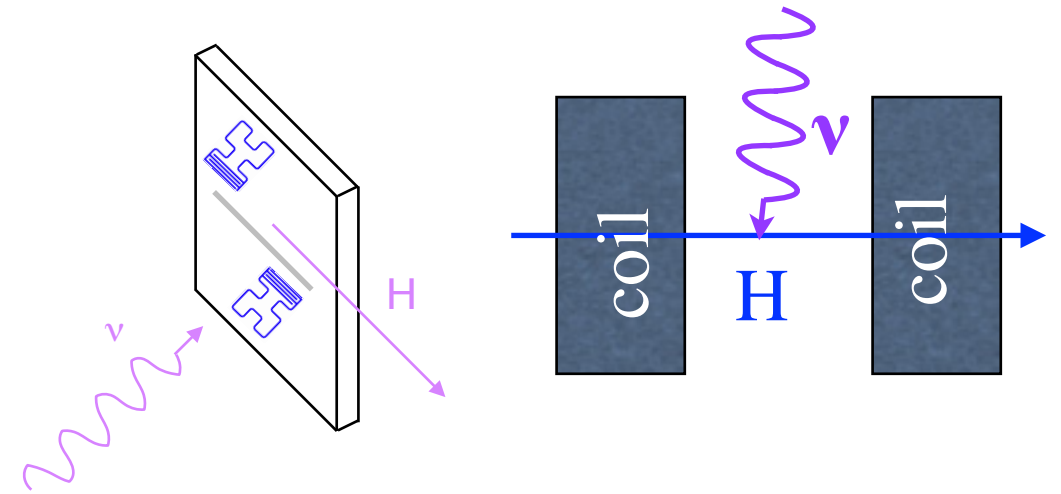
Challenge: make a coil at room temperature,

$r=30\text{cm}$, $I=1\text{A}$, $N=2 \times 10^4$, $H=40\text{mT}$... possible.

Toward a real mm-spectrometer with H-KID

Magnetic field issue for parallel field

$$\text{Helmoltz coil} : H = \frac{\mu_0 I r}{2(z^2 + r^2)^{3/2}} N$$



I: current, r: coil diameter,
z: distance between coils,
N: number of turns per coil

For a coil at room temperature:

r=30cm, z=30cm I=1A, N=2x10⁴, **H= 50mT ... far from 1 T**

Actual Helmotz coil at 100mK-stage:

r~60mm, z~12mm I_{max}=350mA, N~7x10³, **H_{max}= 63mT**

(with formula H=400mT)

Toward a real mm-spectrometer with H-KID

Actual Helmotz coil at 100mK-stage:

Internal diameter $\sim 60\text{mm}$ and $H_{\text{max}} = 63\text{mT}$

For Al 15nm: $2\Delta_0 = 110\text{ GHz}$, $H_c = 40\text{mT}$

For $H = 35\text{mT} < 63\text{mT}$, $2\Delta_{\text{min}} = 55\text{ GHz}$.

Perspectives:

- e-beam lithography a (small) array of KID with width $w = 200\text{nm}$
- Test the H-KID spectroscopic response
- Test oscillating H at Hz-frequency

Conclusion

Toward a real mm-spectrometer with H-KID ?

YES . . . most probably

- Challenge1: e-beam lithography (large) array of KIDs
- Challenge2: produce magnetic coil with $H=35\text{mT}$, for room temperature or for cryogenic environment

Publications on sub-gap KID:

O. Dupré et al, Superconductor Science and Technology, 30, 045007 (2017). [[SUST](#), [ArXiv](#)]
F. Levy-Bertrand et al, Physical Review Applied 15, 044002 (2021). [[PRApplied](#), [ArXiv](#)]

Tuning 2Δ with current: the iKID concept... arXiv:2302.12732, section 3.3

Conclusion

Toward a real mm-spectrometer with H-KID ?

YES . . . most probably

- Challenge1: e-beam lithography (large) array of KIDs
- Challenge2: produce magnetic coil with $H=35\text{mT}$,
for room temperature or for cryogenic environment

THANK YOU

Publications on sub-gap KID:

O. Dupré et al, Superconductor Science and Technology, 30, 045007 (2017). [[SUST](#), [ArXiv](#)]
F. Levy-Bertrand et al, Physical Review Applied 15, 044002 (2021). [[PRApplied](#), [ArXiv](#)]

Tuning 2Δ with current: the iKID concept... arXiv:2302.12732, section 3.3